EE-557
Semiconductor devices I

Three terminal MOSFET

Génie Electrique et Electronique
Master Program
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Outline of the lecture

MOSFET properties

- Device characteristics
- Inversion layer transport and mobility

References:

- J. A. del Alamo, course materials for 6.720J Integrated Microelectronic Devices, Spring 2007. MIT OpenCourseWare (http://ocw.mit.edu/)

Key questions

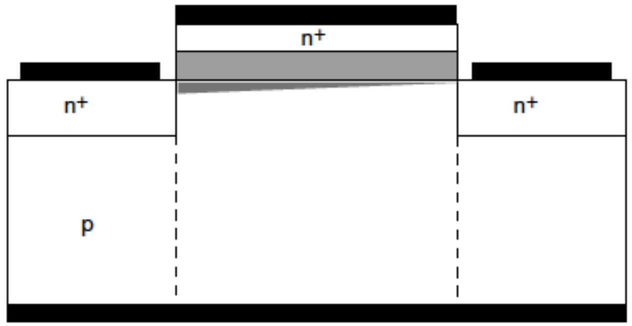
- How does lateral transport through the inversion layer take place?
- What are the most important regimes of operation of a MOSFET?
- What are the key functional dependencies of the MOSFET drain current on the gate and drain voltage?
- Why under some conditions does the drain current saturate?

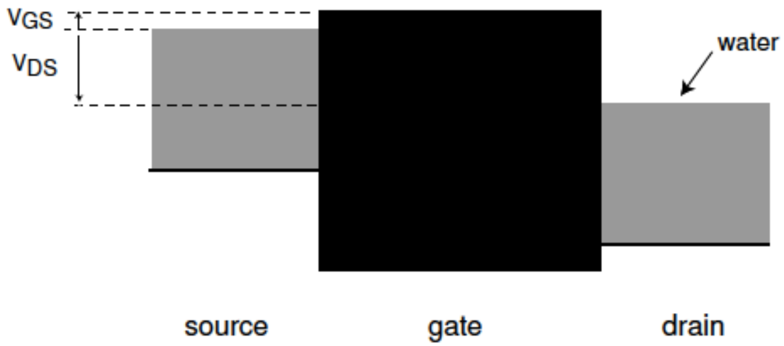
Qualitative operation of the ideal MOSFET

Useful aspect of MOSFETs: Ability to create an inversion layer independent from the rest of the structure

Water analogy of MOSFET:

- Source: water reservoir
- Drain: water reservoir
- Gate: gate between source and drain reservoirs





We want to understand MOSFET operation as a function of:

- gate-to-source voltage (gate height over source water level)
- drain-to-source voltage (water level difference between reservoirs)

Initially consider source tied up to body (substrate or back).

Qualitative operation of the ideal MOSFET

Three regimes of operation:

Cut-off regime:

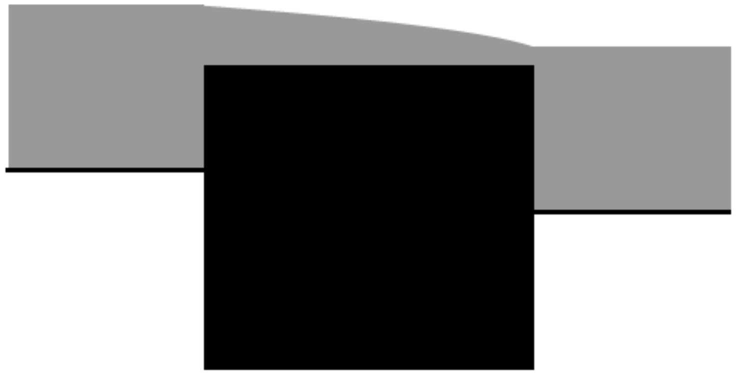
- MOSFET: $V_{GS} < V_T$, $V_{GD} < V_T$ with $V_{DS} > 0$.
- Water analogy: gate closed; no water flows regardless of relative height of source and drain.

$I_D = 0$

cut-off

Qualitative operation of the ideal MOSFET

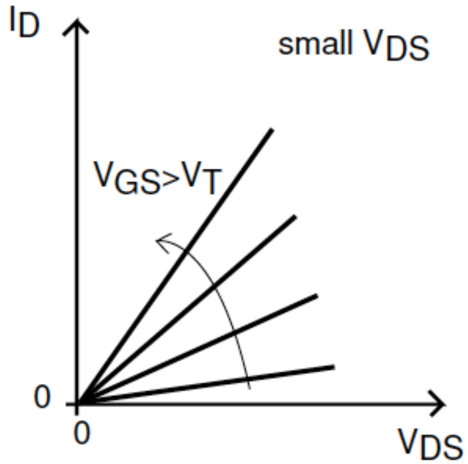
Linear (or Triode) regime:
MOSFET: $V_{GS} > V_T$, $V_{GD} > V_T$, with $V_{DS} > 0$.
Water analogy: gate open but **small difference in height between source and drain**; water flows.

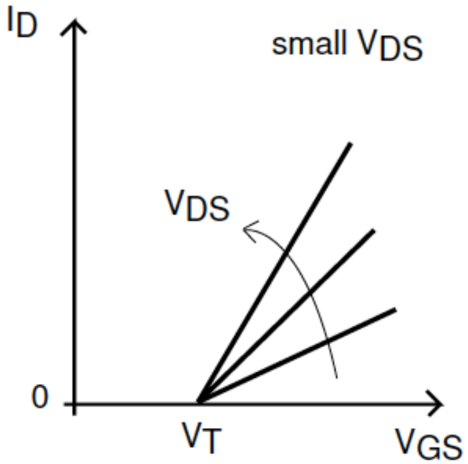


linear or triode

Electrons drift from source to drain
⇒ electrical current!

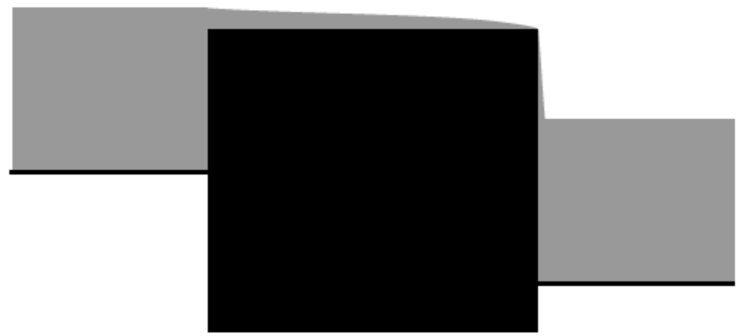
- $V_{GS} \uparrow \rightarrow \; |Q_i| \uparrow \rightarrow \; I_D \uparrow$
- $V_{DS} \uparrow \rightarrow \; \mathcal{E}_y \uparrow \rightarrow I_D \uparrow$





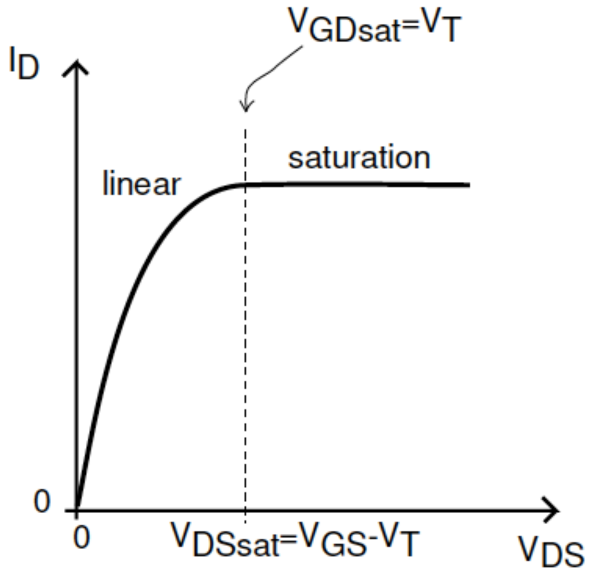
Qualitative operation of the ideal MOSFET

Saturation regime:
MOSFET: $V_{GS} > V_T$, $V_{GD} < V_T$ ($V_{DS} > 0$).
Water analogy: gate open; water flows from source to drain, but free-drop on drain side
⇒ total flow independent of relative reservoir height!



Electrons drift from source to drain ⇒ electrical current!

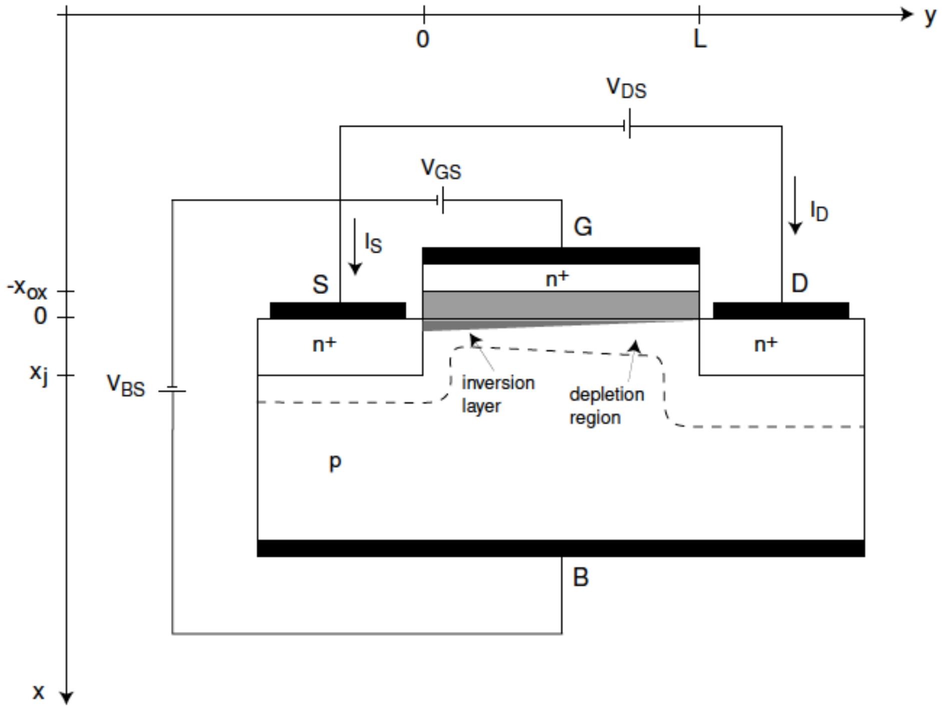
saturation



I_D independent of V_{DS}: $I_D = I_{Dsat}$

Inversion layer transport

Want a formalism to describe lateral current along inversion layer.



Sheet charge approximation

Not interested in details of electron distribution in depth (along x).
Define sheet carrier concentration:

$$n_s(y) = \int_0^\infty n(x,y)dx \qquad [cm^{-2}]$$

General expression for inversion layer current:

$$I_e \simeq -qWv_{ey}(y)n_s(y)$$

Note: I_e independent of y.

Inversion layer transport

Define sheet charge density of inversion layer:

$$Q_i(y) = -qn_s(y) \qquad [C/cm^2]$$

Thus

$$I_e \simeq W v_{ey}(y) Q_i(y)$$

This is the sheet charge approximation (SCA)

- It is meaningful to define an average lateral velocity for electrons
- SCA is valid if vey does not change too rapidly in depth

Under low lateral field:

$$v_{ey}(y) \simeq -\mu_e \mathcal{E}_y(y)$$

Thus

$$I_e \simeq -W \mu_e \mathcal{E}_y(y) Q_i(y)$$

Inversion layer transport

Definition of V(y)

$$V(y) = \phi_s(y) - \phi_s(y=0)$$

The source (located at y = 0) is the reference for V

The lateral electric field along the inversion layer is:

$$\mathcal{E}_y(y) = -\frac{dV(y)}{dy}|_y$$

Thus:

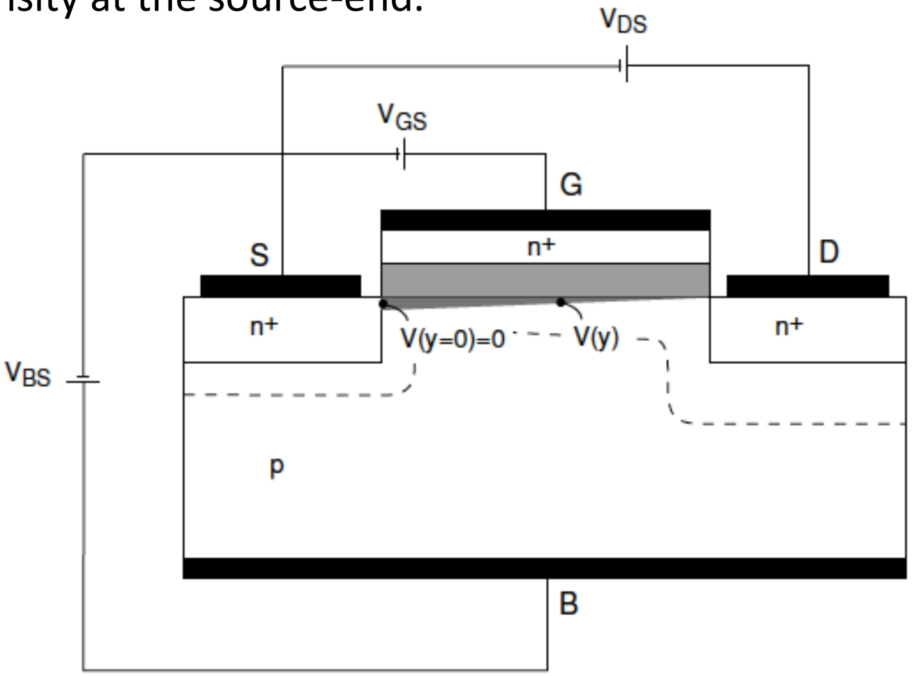
$$I_e = W\mu_e Q_i(y)\frac{dV(y)}{dy}|_y$$

Now we need to relate $Q_i(y)$ with V(y)

Remember fundamental **charge-control relationship** for inversion layer in two-terminal MOS structure:

$$Q_i = -C_{ox}(V_G - V_T)$$

In MOSFET, this equation only applies at source end, where V(0) = 0.
Thus Q_i is the charge density at the source-end.



For rest of the channel, reuse this relationship accounting for local potential drop:

$$Q_i(y) \simeq -C_{ox}[V_{GS} - V(y) - V_T]$$

Q_i depends on y through local inversion layer voltage V(y).

Inversion layer transport

This is called the **gradual-channel approximation (GCA).**

GCA allows break up of 2D electrostatics problem into two simpler quasi-1D problems:

- vertical electrostatics control inversion layer charge
- lateral electrostatics control lateral flow of charge.

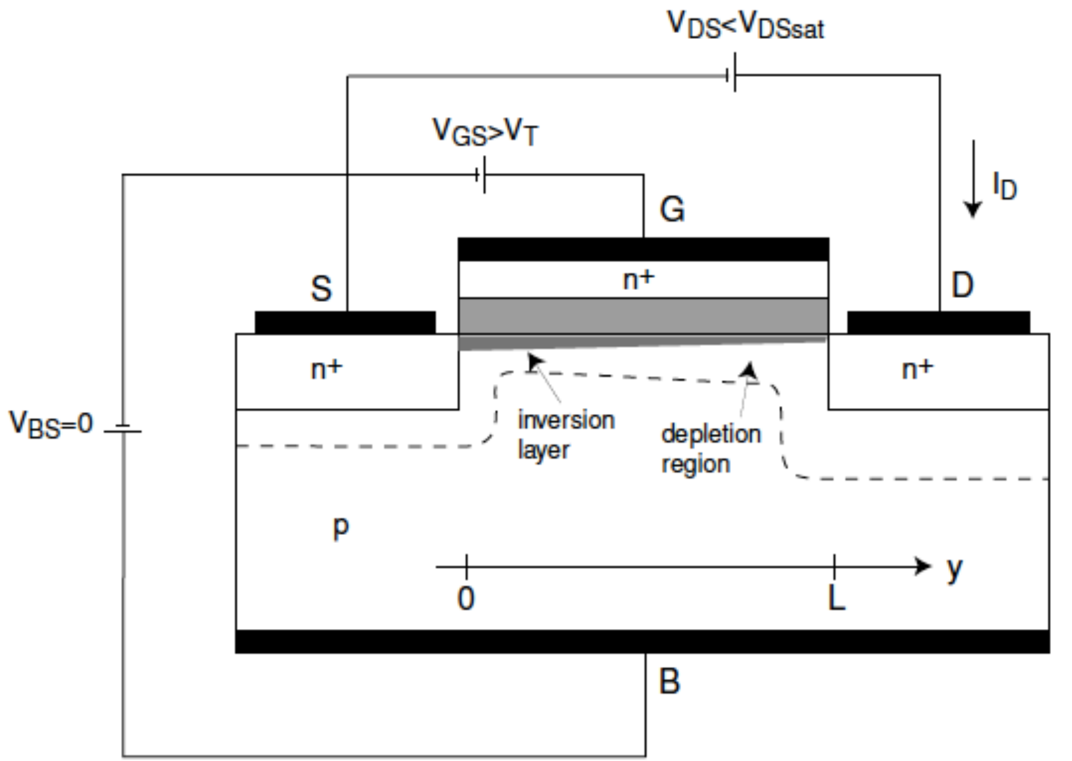
Note: V_T is function of y through body effect

Under GCA, current equation becomes:

$$I_e = -W\mu_e C_{ox}[V_{GS} - V(y) - V_T]\frac{dV(y)}{dy}|_y$$

I-V characteristics of ideal MOSFET

Consider MOSFET in linear regime ($V_{GS} > V_T, V_{GD} > V_T$):



Inversion layer everywhere under gate.

Lateral field set up along channel → current flows.

Electrons drift from source to drain ⇒ electrical current!

- $V_{GS} \uparrow \rightarrow \ |Q_i| \uparrow \rightarrow \ I_D \uparrow$

- $V_{DS} \uparrow \rightarrow \ \mathcal{E}_y \uparrow \rightarrow I_D \uparrow$

I-V characteristics of ideal MOSFET

Separate variables:

$$I_e dy = -W\mu_e C_{ox}(V_{GS} - V - V_T)dV$$

Integrate from $y = 0$ ($V = 0$) to $y = L$ ($V = V_{DS}$):

$$I_e \int_0^L dy = -W\mu_e C_{ox} \int_0^{V_{DS}} (V_{GS} - V - V_T)dV$$

To get:

$$I_e = -\frac{W}{L}\mu_e C_{ox}(V_{GS} - \frac{1}{2}V_{DS} - V_T)V_{DS}$$

Terminal drain current:

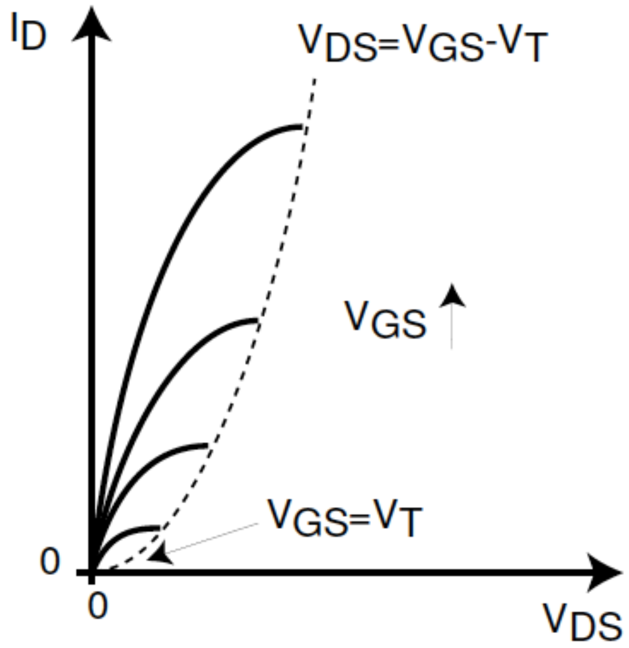
$$\boxed{I_D = -I_e = \frac{W}{L}\mu_e C_{ox}(V_{GS} - V_T - \frac{1}{2}V_{DS})V_{DS}}$$

Result valid as long as strong inversion prevails in all points of channel. Worst point: $y = L$, for which:

$$Q_i(y = L) = -C_{ox}(V_{GS} - V_{DS} - V_T)$$

Therefore, need $V_{DS} < V_{GS} - V_T$, or $V_{GD} > V_T$.

I-V characteristics of ideal MOSFET

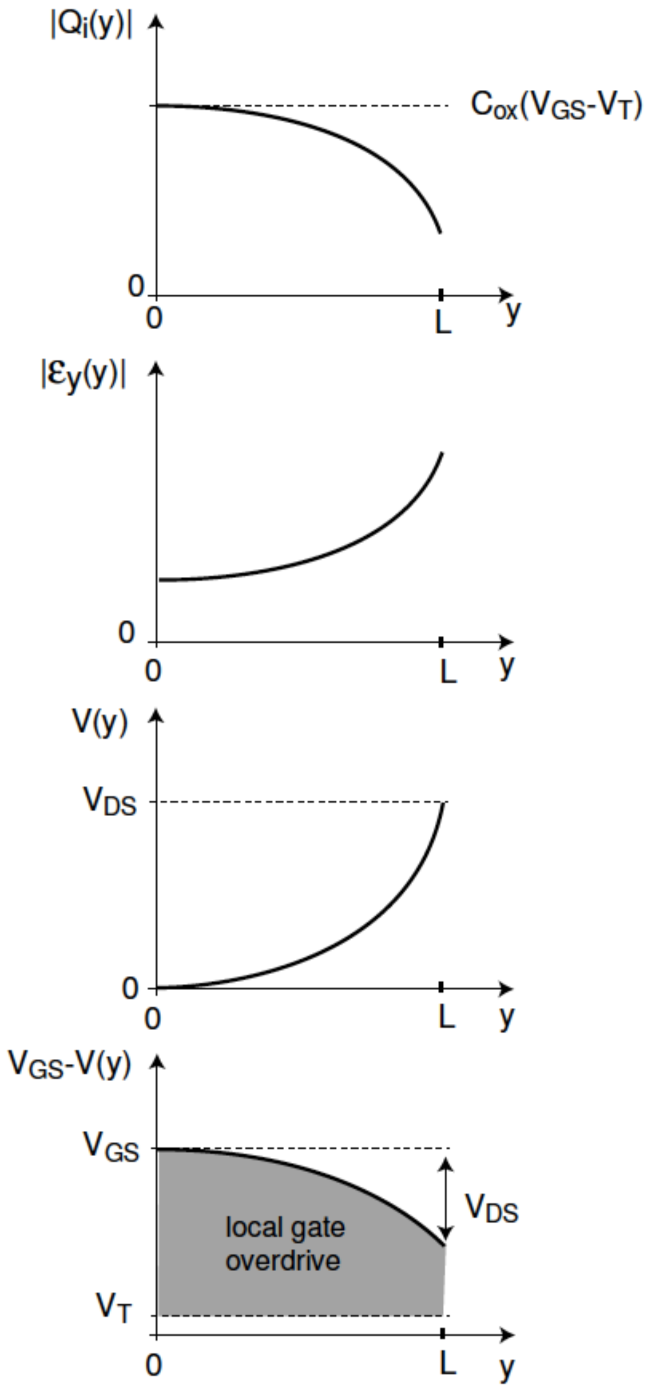


$$I_D = \frac{W}{L}\mu_e C_{ox}(V_{GS} - V_T - \frac{1}{2}V_{DS})V_{DS}$$

Key dependences of I_D in linear regime:

- $V_{DS} = 0 \;\Rightarrow\; I_D = 0$ for all V_{GS}.
- For $V_{GS} > V_T$: $V_{DS} \uparrow \Rightarrow\; I_D \uparrow$ (but eventually I_D saturates).
- For $V_{DS} > 0$ and $V_{GS} > V_T$: $V_{GS} \uparrow \Rightarrow\; I_D \uparrow$.
- For $V_{GS} = V_T \;\Rightarrow\; I_D = 0$

Study lateral electrostatics



Along channel from source to drain:

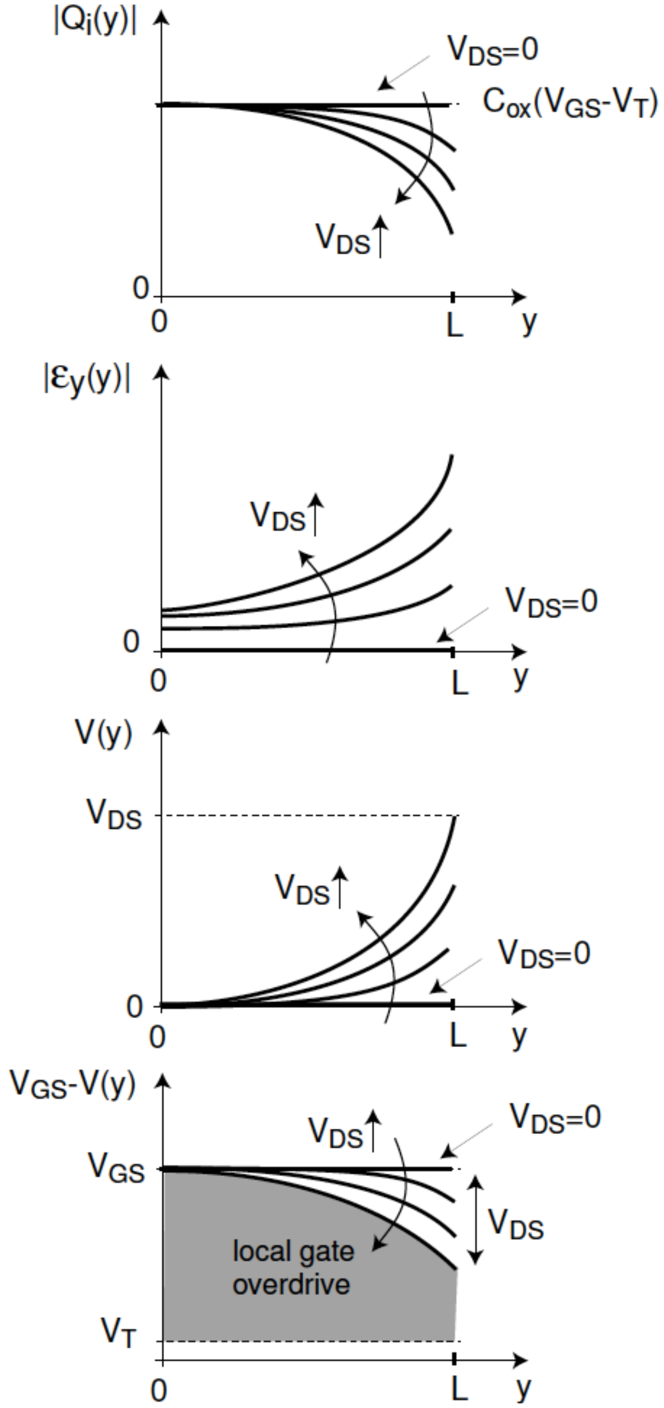
$$V \uparrow \Rightarrow \; V_{GS} - V(y) - V_T \downarrow \Rightarrow \; |Q_i| \downarrow \Rightarrow \; |\mathcal{E}_y(x=0)| \uparrow$$

Local overdrive on gate reduces close to the drain.

Study lateral electrostatics

Impact of V_{DS}:

As V_{DS} ↑ channel debiasing is more prominent.



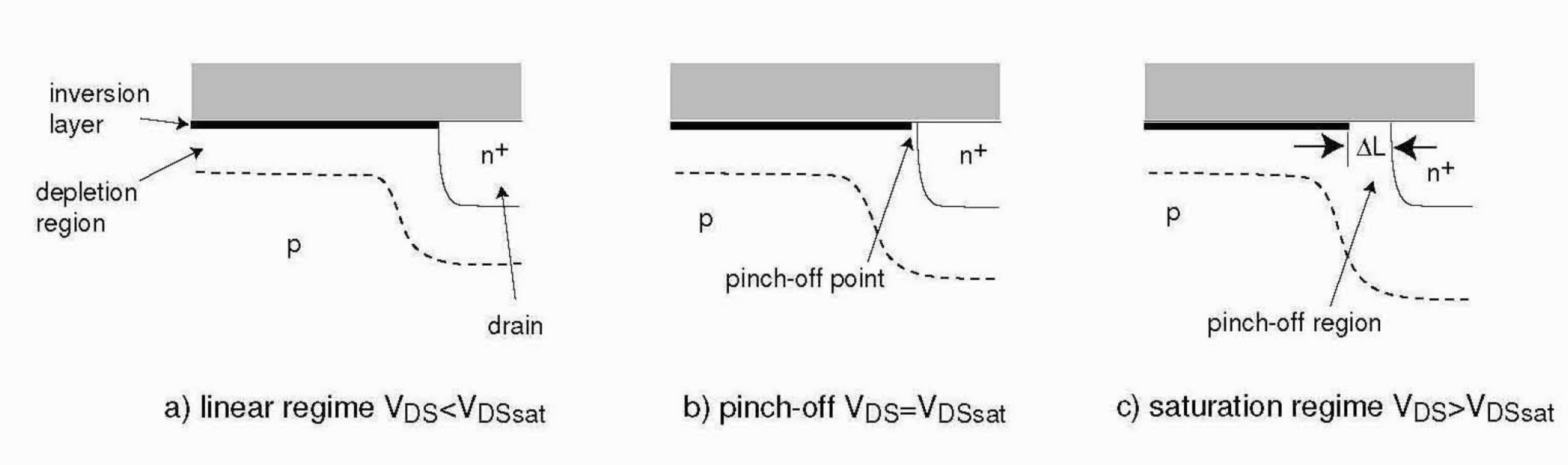
Saturation

What happens if V_{DS} reaches or exceeds V_{GS}-V_T?

Electron concentration at y = L drops to very small concentrations:
depletion region appears at y = L: pinch-OFF.

Depletion region is not barrier to electron flow:

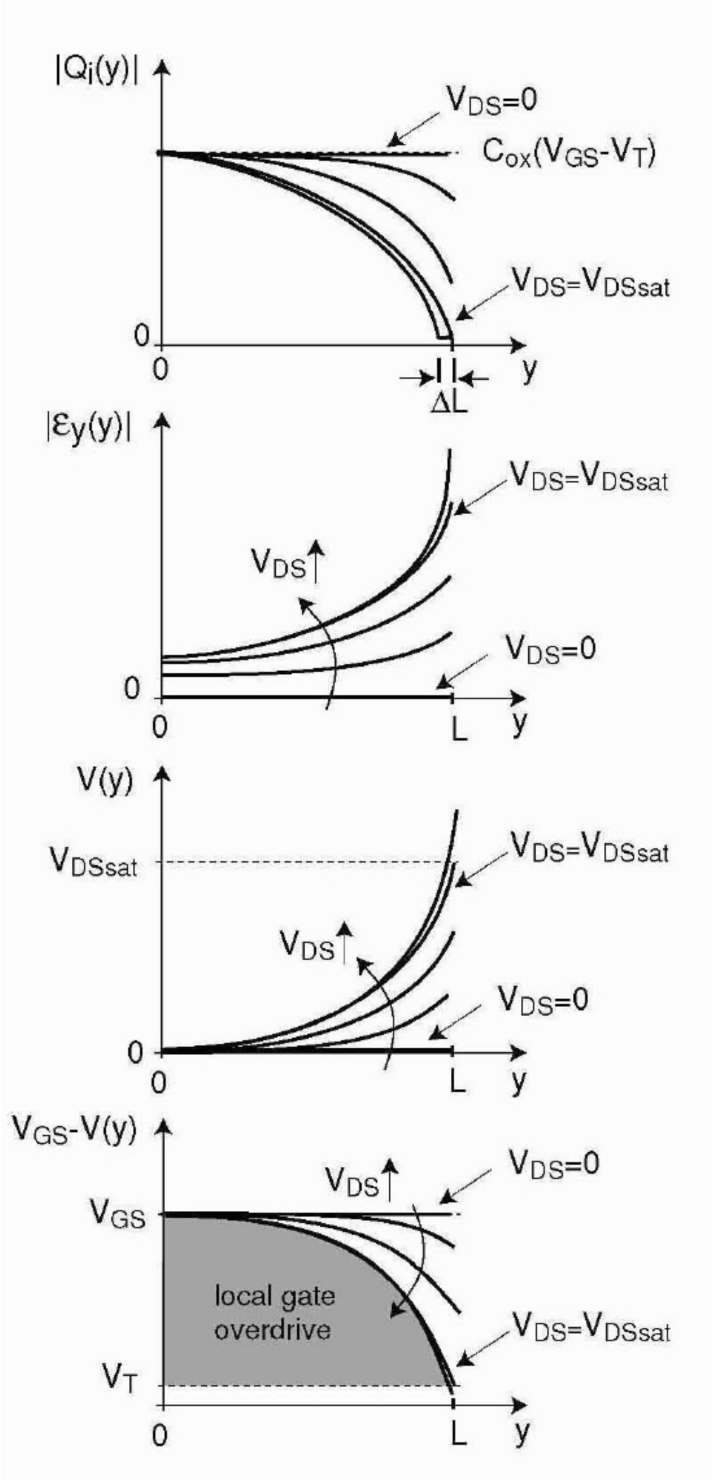
Large electric field region.
Field "pulls" electrons into drain.



- As V_{DS} **exceeds** V_{GS}-V_T, **depletion region widens** into channel underneath gate;
- **All extra voltage consumed in depletion region**;
- Electrostatics of channel, to first order, unperturbed;
- **Channel current unchanged**: MOSFET in **saturation**.

Saturation

Lateral electrostatics in saturation:



Saturation

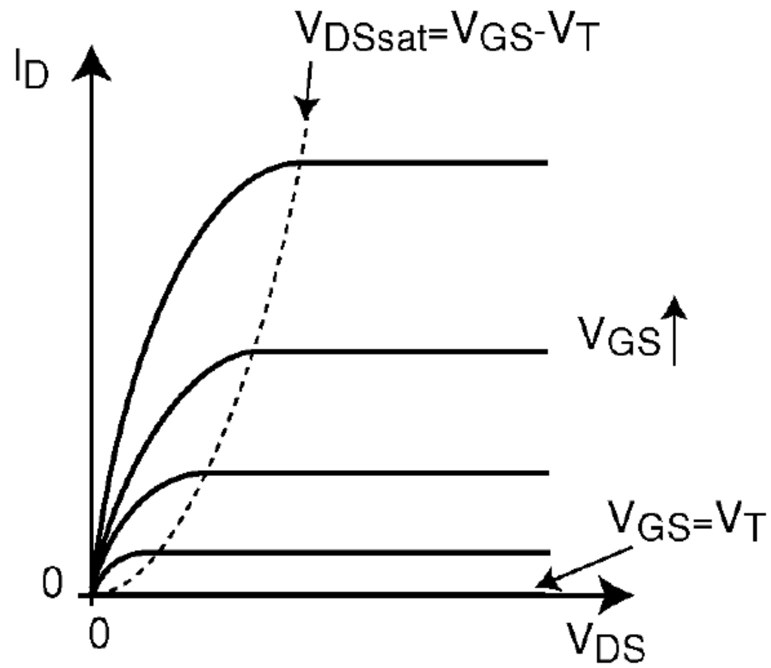
Current model in saturation: **I_D does not increase passed $V_{DS} = V_{GS} - V_T$.**
Hence,

$$\boxed{I_{Dsat} \simeq I_D(V_{DS} = V_{GS} - V_T) \simeq \frac{W}{2L}\mu_e C_{ox}(V_{GS} - V_T)^2}$$

V_{DS} at which transistor saturates is denoted as V_{DSsat}

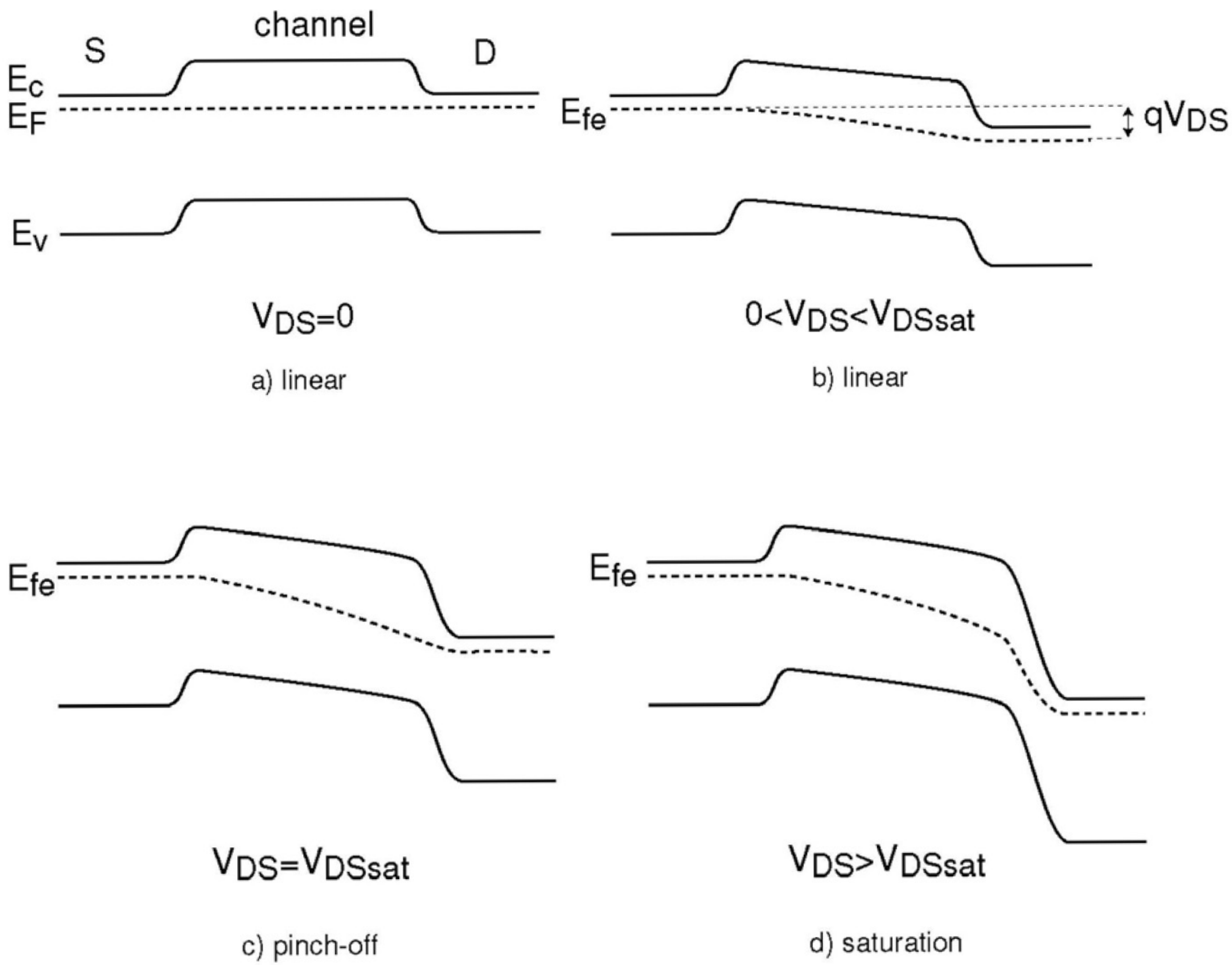
$$V_{DSsat} = V_{GS} - V_T$$

Current-voltage characteristics:



Saturation

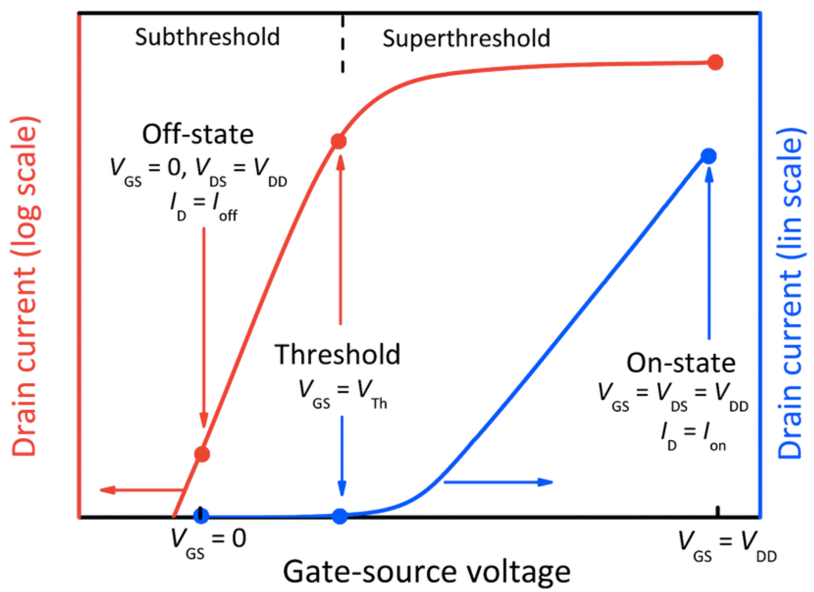
Energy band diagrams ($V_{GS} > V_T$):



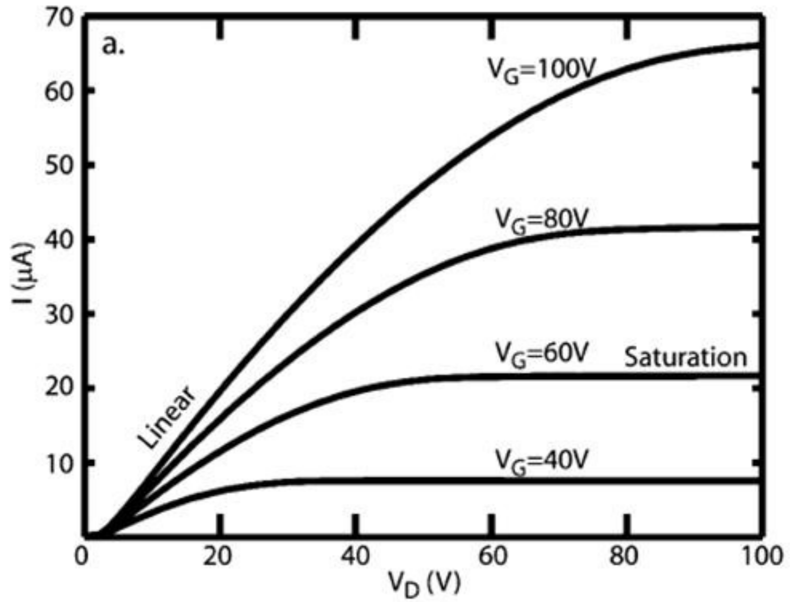
Pinch-off point: region of "free fall" of electrons

Output curves from MOSFETs

Transfer characteristics



Output characteristics



$$\boxed{I_D = \frac{W}{L}\mu_e C_{ox}(V_{GS} - V_T - \frac{1}{2}V_{DS})V_{DS}}$$

Transconductance

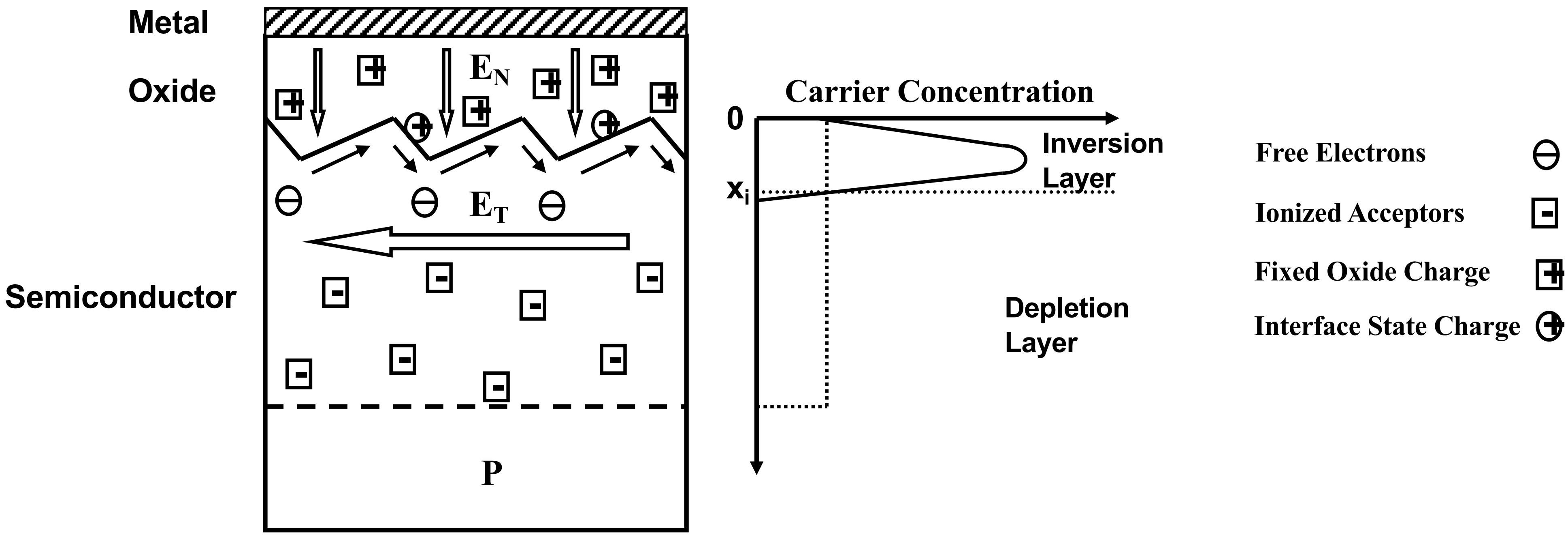
$$g_m = \left.\frac{\partial I_D}{\partial V_{GS}}\right|_{V_{DS}} = \frac{W}{L}C_{OX}\mu V_{DS} \quad \text{linear}$$

$$g_m = \left.\frac{\partial I_D}{\partial V_{GS}}\right|_{V_{DS}} = \frac{W}{L}C_{OX}\mu\left(V_{GS} - V_T\right) \quad \text{saturation}$$

Output conductance
(equal to 0 in saturation)

$$g_D = \left.\frac{\partial I_D}{\partial V_{DS}}\right|_{V_{GS}} = \frac{W}{L}C_{OX}\mu\left(V_{GS} - V_T\right)$$

Estimating Channel Mobility



Field-Effect Mobility: $$\mu_{FE} = \frac{L}{WC_{OX}V_D}\frac{dI_D}{dV_G}$$ *From transconductance*

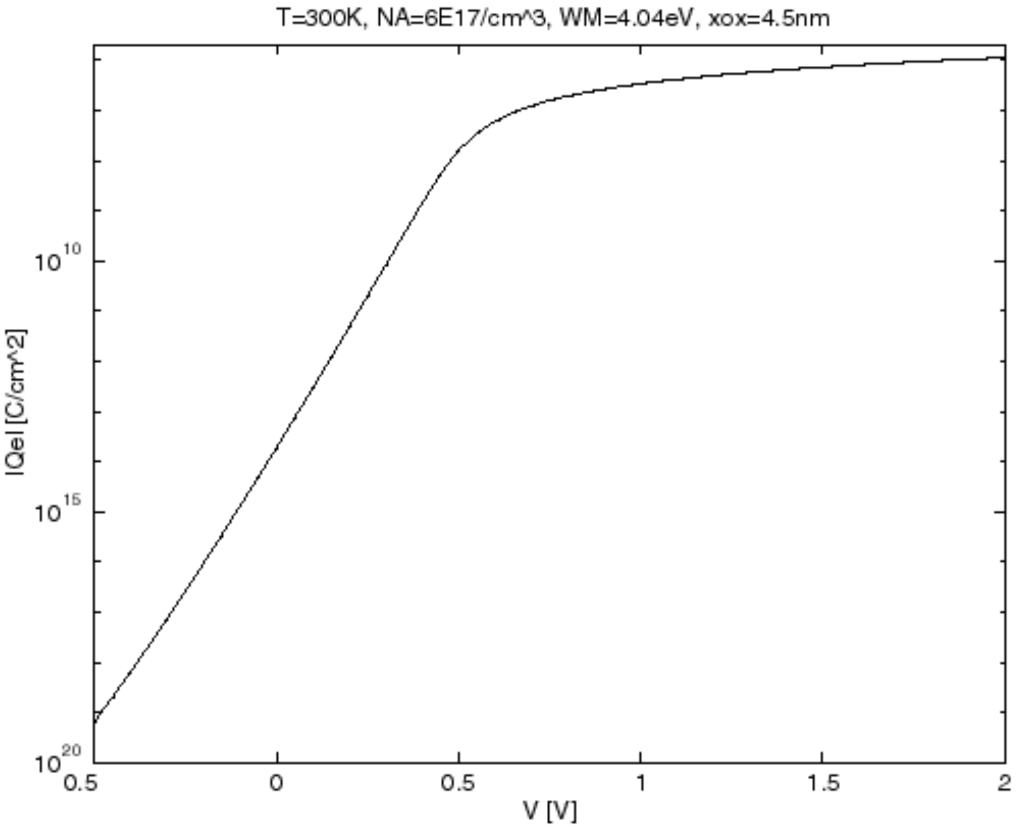
Effective Mobility: $$\mu_{EFF} = \frac{L}{WC_{OX}\left(V_G - V_T\right)}\frac{dI_D}{dV_D}$$ *From output conductance*

B.J. Baliga, *Fundamentals of Power Semiconductor Devices*, Springer 2008

Sub-threshold regime

In MOSFETs: current with the device nominally OFF, that is, for $V < V_{th}$:

Sub-threshold current
MOS structure in depletion but finite electron concentration at surface:



Compute Q_e in depletion:

$$Q_e \simeq -\frac{kT}{q}\frac{n_i^2}{N_A^2}\sqrt{\frac{q\epsilon_s N_A}{2\phi_s}}\exp\frac{q\phi_s}{kT}$$

Key characteristic of subthreshold regime is inverse subthreshold slope:

$$S = n\frac{kT}{q}\ln 10$$

At best, if n =1, **S =60 mV/dec** at room temperature. Typically, S =80-100 mV/dec.

Key conclusions

Sheet-charge approximation: inversion layer very thin in scale of vertical dimensions
⇒ current formulation in terms of Q_i.

Gradual-channel approximation: electric field changes relatively slowly along channel
⇒ GCA breaks 2D electrostatics problem into two quasi-1D problems:

- vertical electrostatics control inversion layer charge
- lateral electrostatics control lateral flow of charge

Consequence of GCA: local inversion layer sheet-charge density: $Q_i(y) \simeq -C_{ox}[V_{GS} - V(y) - V_T]$

In **linear regime**, I_D modulated by V_{GS} and V_{DS}:

V_{GS},to first order, controls electron concentration in channel
V_{DS}, to first order, controls lateral electric field in channel

MOSFET current in **linear regime**:
$$I_D = \frac{W}{L}\mu_e C_{ox}(V_{GS} - V_T - \frac{1}{2}V_{DS})V_{DS}$$

MOSFET current in **saturation regime**:
$$I_{Dsat} = \frac{W}{2L}\mu_e C_{ox}(V_{GS} - V_T)^2$$

V_{DS} that saturates transistor
$$V_{DSsat} = V_{GS} - V_T$$